

Adaptive Foraging in Dynamic Environments Using Scale-Free Interaction Networks

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2 ABSTRACT

3 Group interactions are widely observed in nature to optimize a set of critical collective behaviors,
4 most notably sensing and decision making in uncertain environments. Nevertheless, these
5 interactions are commonly modeled using local (proximity) networks, in which individuals interact
6 within a certain spatial range. Recently, other interaction topologies have been revealed to
7 support the emergence of higher levels of scalability and rapid information exchange. One
8 prominent example is scale-free networks. In this study, we aim to examine the impact of scale-
9 free communication when implemented for a swarm foraging task in dynamic environments. We
10 model dynamic (uncertain) environments in terms of changes in food density and analyze the
11 collective response of a simulated swarm with communication topology given by either proximity
12 or scale-free networks. Our results suggest that scale-free networks accelerate the process of
13 building up a rapid collective response to cope with the environment changes. However, this
14 comes at the cost of lower coherence of the collective decision. Moreover, our findings suggest
15 that the use of scale-free networks can improve swarm performance due to two side-effects
16 introduced by using long-range interactions and frequent network regeneration. The former
17 is a topological consequence, while the latter is a necessity due to robot motion. These two
18 effects lead to reduced spatial correlations of a robot's behavior with its neighborhood and to
19 an enhanced opinion mixing, i.e. more diversified information sampling. These insights were
20 obtained by comparing the swarm performance in presence of scale-free networks to scenarios
21 with alternative network topologies, and proximity networks with and without packet loss.

22 **Keywords:** swarm robotics, foraging, collective decision-making, scale-free networks, dynamic environments, adaptive swarm

1 INTRODUCTION

23 The efficiency of the information sharing mechanisms used by individuals during group decision processes
24 determines to a large extent the fitness of the group decision. In nature, collective systems consist of a high
25 number of individuals living in large and unknown environments, and needing to perform complex tasks to
26 survive. Among the many examples of collective decision-making is choosing a new site to build their home
27 [1], or deciding among a number of foraging patches [2]. Despite the high diversity of tasks, uncertainty
28 and complexity are common features. Hence, individuals apply information pooling to mitigate uncertainty

29 and increase decision accuracy [3]. Achieving efficient opinion sampling depends to a large extent on the
30 network topology that defines the interaction structure and opinion sharing of these individuals [4, 5]. The
31 use of such network is fundamental for collective decision-making. It is generally exploited at two stages
32 of the process (i) when spreading information on one or multiple stimuli that are initially perceived by
33 a limited number of individuals that are able to trigger the collective decision process—e.g. a predator
34 attack—; and (ii) when spreading the individuals' opinions or choices to achieve consensus [6].

35 In artificial systems such as swarm robotics, collective decision-making is mostly designed in static
36 environments [7], where options and their qualities are defined at the beginning and do not change over time.
37 In these studies the focus is mainly on the design of efficient voting mechanisms that enable a high level
38 of decision coherence within the shortest time possible [4]. Alternatively, other studies were addressing
39 the design of decision strategies that tackle the accuracy vs. speed trade-off [8]—i.e. taking longer time to
40 gather enough information and making more accurate decisions vs. exploiting the available information
41 and taking the decision as soon as possible. In both cases, the speed of converging on a decision is a
42 fundamental goal in the design of decision-making. The decision speed strongly depends on the interaction
43 topology the individuals are part of, to spread stimuli or opinions during the decision-making process.
44 Interactions in collective systems are frequently modeled using local (i.e. proximity) communication, where
45 the neighborhood of an individual is defined spatially based on their interaction range, i.e. interacting
46 with all peers within the individual's communication radius. Nevertheless, other interaction models such
47 as scale-free networks were revealed in several real-world examples [9, 10]. A comprehensive review
48 on scale-free phenomena in a more general context can be found in [11]. In various works, scale-free
49 networks enable scalable, fast and efficient information transfer. For example, in [12], authors showed how
50 the betweenness centrality scales with the scale-free exponent. Other works showed how the ultrasmall
51 diameter of the scale-free networks contributes to their efficiency in information transmission [13, 14].
52 Finally, scale-free topologies were studied in natural collective systems such as in [15]. In this work, the
53 authors studied starlings flocks and suggest that collective response to predator's attacks may be achieved
54 through scale-free behavioral correlations. Based on these studies, we extend the application of scale-free
55 networks to artificial swarms in order to investigate the role these networks can play in improving a swarm's
56 collective decision-making process.

57 A key aspect of scale-free networks is the presence of hubs—i.e. nodes with a comparably high
58 connectivity degree—[16, 17]. Hubs represent a small percentage of the network nodes, however, their high
59 connectivity leads to a small network diameter. This facilitates efficient communication by enabling any
60 two random nodes to share information over only few hops, resulting in fast information transfer [13]. In
61 this paper, we exploit this critical feature of scale-free networks to help collective systems to faster respond
62 to changes in dynamic environments. In dynamic environments, conditions change over time and hence,
63 the collective system needs to adapt its behavior within a short period of time in order to survive. We refer
64 to this as the collective response time. In our study, this is the time required for the group to collectively
65 change the intensity of its foraging activities as a response to a change in the availability of the food items.

66 Among many examples of collective tasks in natural systems, we select *foraging* [18] and perform our
67 study using a simulated population of swarming robots. Foraging is a complex task used by many species
68 to retrieve food to their homes, but beyond that it is a metaphor for many real-world robotics tasks such
69 as search and rescue, retrieve materials for collective construction and others. In foraging, individuals
70 (robots) need to continuously make a decision between staying at their base or leaving to forage for food
71 items. A large body of literature has been dedicated to investigate foraging in artificial systems such as
72 swarm robotics. These studies have addressed various research questions such as the foraging performance

73 under the influence of physical robot interference [19, 20], the multi-foraging task [21]—i.e. the foraging
74 for different types of items—or consensus achievement [22, 23]. Additionally, some studies have focused
75 on how to optimize the task allocation in foraging using cost functions [24, 25]. Also how to investigate
76 simple probabilistic models that rely on the foraging success probability in achieving an efficient foraging
77 behavior [26]. Other studies have gone further to investigate whether the performance of swarms in the
78 foraging tasks bears a particular characteristic distribution (e.g. a power law) for any of its time or space
79 features [27, 28]. Despite this intensive research effort, foraging of robot swarms in dynamic environments
80 and the influence of different interaction models are still not well understood. However, these questions are
81 paramount, given the prevalence of scale-free phenomena in real-world systems and admitting that most
82 real environments are dynamic. Therefore, in this paper, we focus on the fundamental question of how the
83 integration of a scale-free interaction structure may influence the collective response of simulated swarms
84 to changes in food density within the foraging environment. We approach this question by analyzing
85 the speed and coherence of the collective response to those changes. We begin with defining the robot
86 (microscopic) and the swarm (macroscopic) behaviors in Sec. 2.1 and Sec. 2.3, respectively. The details on
87 generating scale-free networks from local neighborhoods are given in Sec. 2.2. In Sec. 2.4, we describe the
88 experimental setup. Thereafter, in Sec. 3 we compare the collective response of the swarm in presence and
89 absence of scale-free interactions. We discuss our findings that suggest that the use of scale-free interactions
90 can be advantageous due to (i) reduced correlations between a robot's decisions and those of its spatial
91 neighbors and (ii) enhanced information spread through long-range interactions and frequent rewiring of
92 communication links. These insights are obtained by comparing the influence of scale-free networks to
93 scenarios with alternative random networks as well as scenarios that include packet loss. Conclusions are
94 drawn in Sec. 4.

2 METHODS

95 2.1 Robot behavior

96 Robots are placed in an arena that is divided into two areas: the nest and the foraging environment.
97 Inspired by the behavior observed in harvester ants *Pogonomyrmex barbatus* [29, 30], each robot can switch
98 between two essential states: *resting* and *foraging*. In the foraging state, the robot attempts to find a food
99 item inside the foraging environment by performing a pseudo-random walk. In particular, the robot moves
100 on a straight line until it encounters another robot or an obstacle (e.g. a wall), in which case a *collision*
101 *avoidance* maneuver is initiated. By executing this maneuver, the robot attempts to move in the direction
102 of least physical interference, as sensed by its proximity sensors. After executing the collision avoidance
103 maneuver, the robot goes back to its standard motion following a straight line. When the robot encounters a
104 food item, it collects this item and retrieves it back to the nest where the robot rests for a given period of
105 time θ_r .

106 In the resting state, the robot remains inside the nest, which is the only area where communication with
107 other robots can take place. This is inspired by several natural systems, in which the communication occurs
108 mainly inside the nest or the hive [18, 31, 32, 33]. This approach accommodates two relevant properties of
109 foraging systems: (i) it is common that the foraging environment is significantly larger than the nest area,
110 and hence, individual encountering rates outside the nest are negligibly low. (ii) Due to the high density of
111 individuals inside the nest there is a high likelihood of interaction between individuals that have explored
112 different parts of the foraging environment, and hence a more diversified sample of information about the
113 environment can be collected.

114 Robots can communicate only with neighbors that are within a direct line of sight, sharing their individual
 115 experiences. This is a continuous process—i.e. each robot broadcasts at every time step its previous
 116 experience (success or failure in finding a food item) until it switches again to the foraging state. Continuous
 117 communication activity is a required choice of the experiment design to research the role of network
 118 topology in the emergent behavior [28].

All robots, in our study, are identical and each robot is a probabilistic finite state machine. In particular, a robot's behavior is shaped by two switching probabilities that describe at every time step the robot's likelihood to switch from foraging to resting ($P_{f \rightarrow r}$) or the opposite ($P_{r \rightarrow f}$). These probabilities are updated differently at the robot's resting and foraging states. At the foraging state, the switching probabilities are updated using the robot's foraging experience. The impact of this experience on the robot's decision-making is given by the set of two individual cues $\{i_f, i_r\} \in \mathbb{R}_0^+ \times \mathbb{R}_0^+$. More specifically, the cue i_f defines a numerical value by which the probability to switch from resting to foraging ($P_{r \rightarrow f}$) is increased when the robot has experienced foraging success—i.e. a discovered food item during the latest foraging attempt. The same value is used to decrease this switching probability in case of a failed foraging attempt, i.e. when the robot has spent a specific time (θ_f) foraging without finding a food item. The cue i_r updates the robot's switching probability from foraging to resting ($P_{f \rightarrow r}$) in a manner that is inverse to i_f . Besides updating the switching probabilities at the foraging state, the robot updates those while resting. This update is performed using the experience received from the robot's neighbors and is numerically given by two social cues $\{s_f, s_r\} \in \mathbb{R}_0^+ \times \mathbb{R}_0^+$. The social cue s_f is used to update the switching probability from resting to foraging (i.e. $P_{r \rightarrow f}$) by increasing (decreasing) $P_{r \rightarrow f}$ when the robot's neighbors report primarily on successful (failed) foraging attempts. Whereas, s_r is used to update the switching probability from foraging to resting (i.e. $P_{f \rightarrow r}$), inversely to s_f . In the following we define how the switching probabilities are updated at every simulation step (as described in [28]; to prevent divergence, both probabilities were truncated between zero and one):

$$P_{r \rightarrow f}(t + 1) = P_{r \rightarrow f}(t) + \delta_\eta(t)s_f + \delta_\phi(t)i_f \quad (1)$$

$$P_{f \rightarrow r}(t + 1) = P_{f \rightarrow r}(t) - \delta_\eta(t)s_r - \delta_\phi(t)i_r, \quad (2)$$

119 where $\delta_\eta(t)$ is the difference between the successful and the failed foraging attempts communicated to the
 120 robot by its neighbors. Hence, it has a positive sign when there are more successful attempts than failed
 121 ones and a negative sign otherwise. Consequently, the former increases the switching probability from
 122 resting to foraging and the latter increases the switching probability from foraging to resting. $\delta_\eta(t) = 0$ if
 123 the robot is not resting. Additionally, the robot's individual experience during a foraging attempt that starts
 124 at t_f is defined as follows:

$$\delta_\phi(t) = \begin{cases} +1, & \text{at } t_{if} \\ 0, & \text{if } t_f < t \leq t_f + \theta_f \text{ \& no item is found} \\ -1, & \text{if } t > t_f + \theta_f \text{ \& the robot is still foraging} \end{cases} \quad (3)$$

125 where t_{if} is the (unique) time step at which the robot finds an item while in foraging state. While in the
 126 foraging state, the robot may find an item at any time $t_f < t_{if}$ (i.e. it could also happen that $t_f + \theta_f < t_{if}$).
 127 After finding an item, i.e. subsequently to t_{if} , the robot leaves the foraging state. If no item is found and
 128 the foraging time crosses the threshold θ_f , then $\delta_\phi(t) = -1$. This increases $P_{f \rightarrow r}(t)$ at every time step
 129 $t > t_f + \theta_f$, guaranteeing that the robot will probabilistically leave the foraging state at some t , even
 130 without finding an item. $\delta_\phi(t) = 0$ outside of the foraging state.

131 The robot behavior is illustrated in Fig. 1 using a state diagram. It includes the following states:
 132 (i) foraging: after having spent at least θ_r time steps resting, the robot switches with probability $P_{r \rightarrow f}$
 133 from resting to foraging. It attempts to search the foraging area for a food item to retrieve to the nest.
 134 If the robot fails to find a food item within a predefined time θ_f , it switches with probability $P_{f \rightarrow r}$
 135 to homing; (ii) homing: in this transitional state the robot returns to the nest, with $\delta_\eta(t) = 0$ and $\delta_\phi(t) = 0$; as
 136 soon as the robot reaches nest, it switches to distancing; (iii) distancing: having returned to the nest, the
 137 robot searches for an empty spot in the nest where it can rest; similar to the homing state, distancing is
 138 a transitional state with $\delta_\eta(t) = 0$ and $\delta_\phi(t) = 0$; distancing terminates after θ_d time steps and the robot
 139 switches to resting; (iv) resting: subsequent to distancing the robot rests for at least θ_r time steps after
 140 which it switches with probability $P_{r \rightarrow f}$ to foraging. A resting robot broadcasts ‘success’ (or ‘failure’) to
 141 its neighbors if the latest foraging attempt was successful (or not), respectively. If the robot failed to leave
 142 the nest in state (i), it has no information about the foraging environment and, thus, does not broadcast any
 143 message. Throughout the entire experiment, the robot performs collision avoidance maneuvers if other
 robots or walls enter its proximity sensors’ range (not shown in Fig. 1 for better readability).

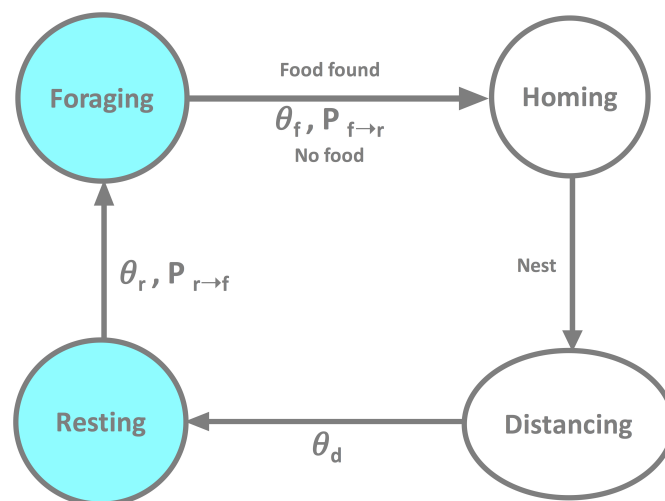


Figure 1. The state transition diagram of a robot performing the foraging task.

144

145 2.2 Robot scale-free communication network

146 In this section, we describe the design and implementation of the algorithm that leads to a scale-free
 147 robot communication network. An implementation of this algorithm in C++ is publicly available online¹
 148 [34]. The generation of a scale-free network from local neighborhoods is an iterative process, where at
 149 each time step t the robot communication is updated according to the following procedure:

- 150 1. Identify all connected components (*CCs*) in the resting swarm using depth-first-search. A *CC* is the
 151 maximal set of nodes (robots), where each two nodes are connected through a finite path. The *CCs* are
 152 initially derived from the spatial networks in which the robots are neighbors if they are within each
 153 other’s communication radius.
- 154 2. Generate the scale-free network topology within a *CC* using preferential attachment [16] as
 155 summarized in Alg. 1. This algorithm is largely inspired by previously proposed approaches [35, 36].

¹ <https://osf.io/48b9h/>

156 We begin by selecting a sink node $\nu_{s,0}$ which is the node with the highest number of neighbors within
 157 its spatial proximity—i.e. within the initial radius of $r_s = 1.25$ m. Within this r_s , each spatial neighbor
 158 $\nu_{s,i}$ is linked to $\nu_{s,0}$, creating an initial sink network G_s . Next, we increase r_s by 0.2 m. Due to this
 159 increase, new nodes ν_{new} enter r_s . Each ν_{new} is connected to any ν_s following preferential attachment.
 160 In a preferential attachment process, the higher the degree of node ν_s compared to the sum of all node
 161 degrees within G_s , the more likely is ν_{new} to connect to ν_s . After all ν_{new} were added to G_s , r_s is
 162 increased again by 0.2 m. This process continues until G_s is of the same size as CC .
 163 3. Repeat 2. for every CC in the swarm.

164 In Alg. 1, N_{sink} is the size of the sink network G_s , in terms of the number of nodes. Similarly, N_{CC}
 165 is the size of the selected connected component; d_s is the degree of node ν_s , and $\sum_i d_i$ is the sum over
 166 all degrees in the sink-network. Note that the robot communication approaches the scale-free network
 167 topology only for large enough CC . However, due to the relatively small area of the nest the robots had a
 168 high tendency to self-aggregate into a giant connected component.

169 To test how successful Alg. 1 was in generating a scale-free topology, we recorded the degree distributions
 170 at $t = 10$ of 1000 simulation runs. At $t = 10$ the large majority of robots was still resting inside the
 171 nest, providing us with at least one large CC . Scale-free networks are characterized by the power law
 172 degree distribution. Thus, we tested whether our recorded degree distributions follow the power law using
 173 previously established statistical methods [37, 28, 38]. Essentially, this statistical analysis is a highly
 174 rigorous power law fitting procedure that consists of three critical steps: (i) testing whether the shape of the
 175 distribution is due to random fluctuations, i.e. testing the *goodness-of-fit* given by a p -value. We proceed to
 176 the next step only if $p < 0.1$, otherwise the power law fit is considered unreliable. (ii) As the power law
 177 behavior is commonly found at the tail of the distribution, we proceed to the third step only if the data
 178 that is fit the power law behavior represents at least 10% of all data points. (iii) Finally, we compare the
 179 power law fit to other common distributions (such as the exponential or the log-normal) that may also tend
 180 to resemble a linear shape on a log-log scale (which is characteristic for the power law) [37, 39]. This is
 181 done by considering the log-likelihood ratio of each pair of distributions, which has a negative value if
 182 the distribution we compare the power law to is a significantly better fit. Consequently, the hypothesis
 183 that the data is power law distributed is not rejected only if this log-likelihood ratio is positive and only if
 184 we did not reject it at steps (i) and (ii). The result of the testing procedure can be captured by a numeric
 185 value to categorize whether the support for the hypothesis is not present, weak, moderate or strong (for
 186 more details see [28]). The test results for Alg. 1 have shown a statistically sound support for the power
 187 law distribution in 76% of tests (we ran 1000 tests), suggesting that Alg. 1 was considerably successful in
 188 creating scale-free networks.

189 Alternatively, one can use Alg. 1 to construct networks with a degree distribution that is less skewed
 190 than power law and more symmetric around the mean degree, i.e. networks that resemble more closely
 191 the well-known small-world networks. To this end, one can simply replace the preferential attachment
 192 component $d_s / \sum_i d_i$ by a real number.

193 2.3 Swarm behavior

194 At the swarm level, the foraging behavior emerges as a result of complex interactions between the robots
 195 as well as between robots and their environment. As mentioned above, we evaluate this performance in
 196 dynamic environments, in which the food density is subject to single and periodic changes. The quality of
 197 the emergent performance is evaluated with respect to the swarm response (adaptivity) to the changing
 198 number of items in the foraging environment. In particular, we define the swarm performance with respect

Algorithm 1: Pseudo-code for the implementation of the preferential attachment, executed at each time step.

```

initialize a sink network  $G_s \subseteq CC$ :
  Choose a node  $\nu \in CC$  with the highest degree and connect it to its spatial neighbors
  within the radius  $r_s$  around  $\nu$ .
while  $N_{sink} < N_{cc}$  do
  increase  $r_s$ 
  for each  $\nu_{new} \in CC$  do
    for each  $\nu_s \in G_s$  do
      create a bi-directional link between  $\nu_{new}$  and  $\nu_s$  with probability  $P_{BA} = d_s / \sum_i d_i$ 
      if no link created then
         $P_{BA} \leftarrow P_{BA} + d_s / \sum_i d_i$ 
      end
    end
  end
end

```

199 to (i) the speed of the swarm's collective response, and (ii) the number of retrieved items. The collective
 200 response is quantified using the number of resting robots at any time step. For instance, in case of a sudden
 201 high availability of food items an ideal swarm's response would be to allocate more robots to the foraging
 202 state shortly after the increase in the number of food items is detected.

203 We borrow the term of settling time from control theory to measure the time of the swarm's collective
 204 response, referred to as the convergence time—i.e. the time the swarm needs to adapt the number of
 205 resting/foraging robots to any change in the items density. The settling time is defined as the time elapsed
 206 from the moment of applying a particular stimulus (i.e. changing the items' density) to the time the system
 207 output (i.e. number of robots N_{rest} that are in the resting state) reaches and remains within a specified
 208 margin of error. Hence, the time to convergence is computed as in the following:

$$t_{conv} = \inf\{S\}, \quad \text{where } S = \{t : |Fn(N_{rest}(t)) - Fn(N_{rest}(t_{steady}))| < \zeta\}, \quad (4)$$

209 where $\inf\{S\}$ is the greatest lower bound of the set S , and the set S includes all time steps t at which
 210 the difference between the transformed number of resting robots at a specific time step $N_{rest}(t)$ and the
 211 transformed number of resting robots at the steady state $N_{rest}(t_{steady})$ is smaller than a threshold ζ . In our
 212 study we set $\zeta = 0.1$. Here, t_{steady} is the time step at which the system reaches its steady state. To compute
 213 the time to convergence, we use the matlab tool STEPINFO², that first applies $Fn(\dots)$ to transform the input
 214 into a continuous representation. This transformation was used for N_{rest} .

215 Finally, in addition to the convergence time, we investigate the swarm performance in terms of the number
 216 of retrieved items. The number of retrieved items is strongly related to the time to convergence, since a
 217 faster convergence implies a higher efficiency in retrieving items. We compute this performance measure
 218 using the cumulative sum of the items retrieved over time.

219 2.4 Simulation setup

220 We ran the simulations using ARGOS³, a well-established physics-based simulator for swarm robotics
 221 [26]. The values of particular parameter settings that can be used to reproduce our simulations and results

² <https://www.mathworks.com/help/control/ref/stepinfo.html>

³ <http://www.argos-sim.info/>

222 are listed in Table 1. Additionally, the reader is encouraged to find our project on the Open Science
 223 Framework⁴ [34] to download the development sources and run the simulations.

224 Figure 2 displays snapshots from simulations with proximity (Figure 2(A)) and scale-free (Figure 2(B))
 225 networks. The square-shaped arena is of the size $L \times L$ ($L = 50$ m) and consists of the nest $A_n = 10 \times 50$ m²
 226 (gray colored floor in Figure 2) in addition to the foraging environment $A_f = 40 \times 50$ m² (white in Figure 2).
 227 Inside the foraging environment, food items are uniformly distributed. When a robot brings a food item to
 228 the nest, a new food item appears at a random location within the foraging environment, preventing item
 229 depletion that might lead the foraging activity to halt.

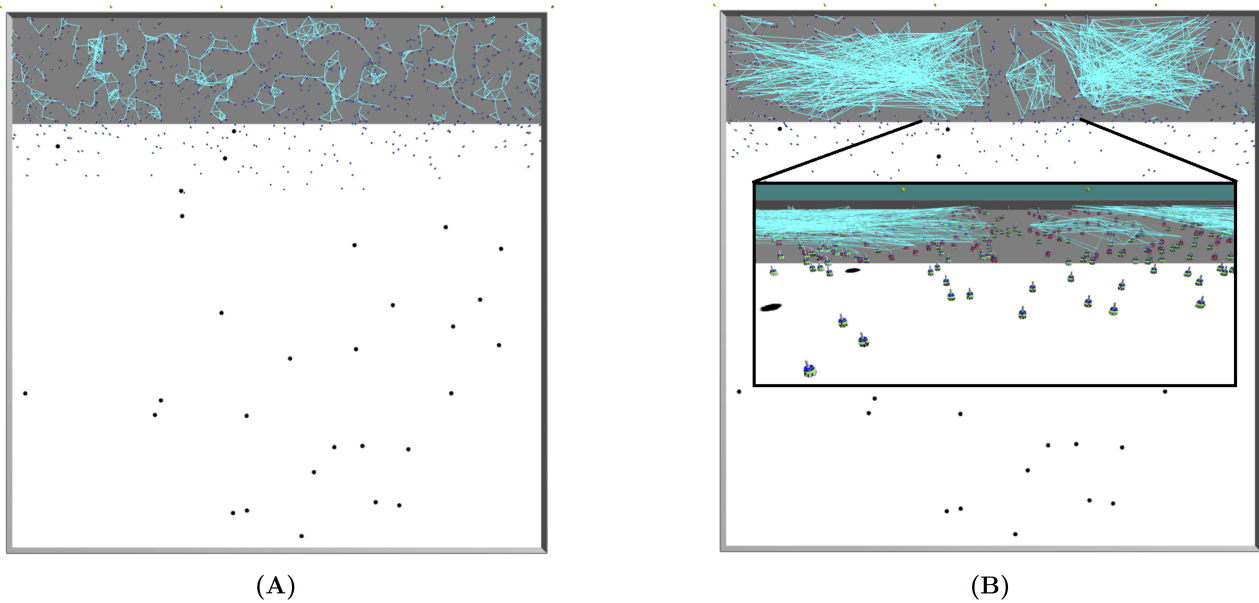


Figure 2. Illustrations of the arena taken from ARGoS simulations. Gray area: nest; white area: foraging environment; black dots: items; blue objects: Footbots; light-blue lines: communication (range-and-bearing) links. Top views onto the entire arena; the communication network is constructed in (A) using spatial network given by the local robot interactions, and in (B) using Algorithm 1; the inset shows a close-up view on the robots. In all figures, the communication links are formed *only* for *resting* robots *inside* the nest, as in our experiments moving robots neither broadcast nor listen to any messages. Therefore, it can happen that although a robot is within the communication range of another, no communication link is established between the two.

230 The robots are able to rapidly leave or return to the nest thanks to the phototaxis behavior. For that
 231 purpose, light beacons are installed on one side of the nest, opposite to the foraging environment (yellow
 232 dots at the top of Figure 2(A) or Figure 2(B)). Robots are repelled from the lights whenever they need to
 233 leave the nest, and attracted to the lights to return to the nest. The swarm consists of N_{robots} homogeneous
 234 robots (we use Footbots [40]). Robots are equipped with probabilistic controllers, which tune their behavior
 235 to forage or rest based on the above mentioned probabilities (i.e., $P_{r \rightarrow f}$ and $P_{f \rightarrow r}$).

236 To implement the proposed networks (i.e. scale-free and proximity), we utilize the range-and-bearing
 237 medium (that includes sensor and actuator) provided in ARGoS. However, this communication medium is
 238 used differently for the two networks. In the case of proximity networks, the communication range of the

⁴ <https://osf.io/48b9h/>

Table 1. Robot and arena parameters.

Parameter	Value
<i>Robot parameters</i>	
Physical avoidance range	0.1 m
Communication range	1.25 m
Maximum moving speed	1 m/s
Minimum resting time θ_r	100 s
Minimum unsuccessful foraging time θ_f	500 s
Minimum distancing time θ_d	100 s
Individual cues i_f, i_r	0.01
Social cues s_f, s_r	{0.01, 0.25, 0.99}
<i>Arena parameters</i>	
Total area of the arena A	$50 \times 50 \text{ m}^2$
Area of the Nest A_n	$10 \times 50 \text{ m}^2$
Area of the Foraging environment A_f	$40 \times 50 \text{ m}^2$
Number of robots N_{robots}	950
Number of items N_{items}	30 or 300
Total experiment duration T	10^4 ts

239 range-and-bearing medium is set to 1.25 m (as we can see in Table 1). In the case of the scale-free networks,
 240 at each time step, we first obtain the connected components using the spatial proximity network, where the
 241 robots communicate via the range-and-bearing medium within a radius of 1.25 m. In the same time step, for
 242 each of these connected components, we create a scale-free network in which the connections can span over
 243 the entire length of the nest, if the connected component spans over that area. Thus, the resulting scale-free
 244 networks can include much longer ranges than 1.25 m. For implementing such a communication topology
 245 in real-world swarms, it is possible to apply other communication systems than the range-and-bearing
 246 medium, such as other radio communication technologies (e.g. the well-established wifi [41]), shared
 247 memory [7] or promising concepts such as the augmented reality for Kilobots (ARK) [42].

3 RESULTS AND DISCUSSION

248 The goal of this study is to investigate the influence of the scale-free topology on the collective performance
 249 and response of a swarm foraging in a dynamic environment. The dynamics of the environment is modeled
 250 in terms of single and periodic changes in the food density. In robot swarms, the interaction among
 251 individuals is mostly modeled using local communications, where each robot has a limited communication
 252 range. The communication range is usually much smaller than the dimension of the world. The robot's
 253 neighborhood is defined as the set (or a subset) of robots that is located within its communication
 254 range. In this study, besides local interactions, we make use of the well-known preferential attachment
 255 mechanism (applied in Alg. 1, see Sec. 2.2) to construct a scale-free topology that accelerates information
 256 sharing. Hence, we investigate whether it may improve the efficiency of the swarm collective response to
 257 environmental dynamics.

258 As mentioned above, we define the collective response in terms of the number of resting robots and
 259 measure it as the change in this number over time. In our experiments, initially, the entire swarm is in the
 260 resting state. In the following, a transient period begins, during which the swarm displays oscillations at the
 261 group level. First, almost all robots begin foraging during the first 500 time steps (ts)—Note that a simulated
 262 time step is one second, with one tick per second. Within the subsequent $\approx 500 \text{ ts}$ most of the swarm
 263 individuals come back to the nest and switch to resting. Even though such collective behavior oscillates

264 over several following time periods—due to the probabilistic nature of the robot controller— the coherence
265 increases rapidly and the swarm converges on a relatively stable number of resting robots. The duration
266 of this transient period is mostly shorter than $5 \cdot 10^3$ ts, after which we begin our measurements. Finally,
267 based on preliminary results, we set the swarm size to $N = 950$, which balances physical interference with
268 swarm performance and delivers a sufficiently large number of samples for statistically sound analysis.

269 We use two experimental settings. In the first setting, after the system converges on a number of resting
270 robots N_{rest} (number of foraging robots is then $N_{forg} = N - N_{rest}$), a single external stimulus is applied.
271 This stimulus represents an increase in the number of food items N_{items} by the factor of 10 (from 30 to 300
272 items) at a particular time point t_{crit} . In the second experimental settings, we challenge the swarm further
273 by applying a periodic change in the density of the food items, hence the benefit of a quicker response
274 becomes clearer. The periodic change is applied over periods of 2500 ts and can be of two types, either
275 increasing or decreasing the number of food items N_{items} , always by a factor of 10.

276 In each of the two experimental settings, two interaction networks are implemented, proximity network
277 (emerging from local interactions), and scale-free network (generated using preferential attachment). As
278 mentioned above, for the construction of scale-free networks, the connected components of the robots
279 resting at the nest site are used to impose the network topology. Over these networks the robots exchange
280 specific information about their success or failure of the latest foraging attempt seeking an accurate
281 estimation of the current situation in the foraging environment.

282 According to our experiments, there are two main cases, in which the influence of the communication
283 topology is negligible. These are (i) small social cues (i.e. with s_f and s_i values smaller than 0.01),
284 and (ii) small number of resting robots N_{rest} . The first case is straightforward, as the social cues
285 decrease, the impact of the information obtained from other robots decreases, and hence the impact
286 of the interaction network on the emergent dynamics vanishes. The second case is associated with the
287 particular implementation of the scale-free communication network in the nest. Since the construction
288 of this network relies on the connected components present in the nest at every time step, small numbers
289 of resting robots result in scaling down the size of such connected components and hence topological
290 contribution becomes negligible. Therefore, as we aim to investigate the influence of the interaction
291 network on the emerging dynamics, we consider those cue configurations in which the social feedback
292 of the robot's neighborhood has a distinguishable role in shaping its decision. This is achieved by setting
293 the social cues to have a clear advantage over the individual cues—i.e. $s_f \gg i_f$, $s_r \gg i_r$. For an extensive
294 discussion on the impact of cue values on swarm behavior in a similar settings of the foraging task
295 the interested reader is referred to [18, 28]. For the reasons mentioned above, we set the cue values to
296 $s_f = 0.25$, $s_r = 0.25$, $i_f = 0.01$, $i_r = 0.01$. Nevertheless, further below we will additionally compare
297 our results to those obtained with more extreme values of the social cues, i.e. $s_f = 0.01$, $s_r = 0.01$ and
298 $s_f = 0.99$, $s_r = 0.99$.

299 The plots in Fig. 3 depict results obtained over 30 runs. They compare the emergent collective response of
300 the swarm to a single stimulus (i.e. change in food density) as well as to multiple stimuli when individuals
301 interact locally in comparison to interacting via scale-free topologies. Firstly, our results reveal a clear
302 impact of the network structure on the robot activation level across all types of stimuli (i.e. increasing or
303 decreasing food item density). This is illustrated through the number of resting robots being considerably
304 smaller when using the scale-free network as opposed to the proximity network throughout the entire
305 simulation time (see Fig. 3A and B). Proximity networks in Fig. 3B show a non-adaptive swarm behavior
306 that is largely due to the very low number of foraging robots. When there are too few foraging robots, the
307 system tends to approach a global absorbing state in which robots cease to switch to foraging. In case of

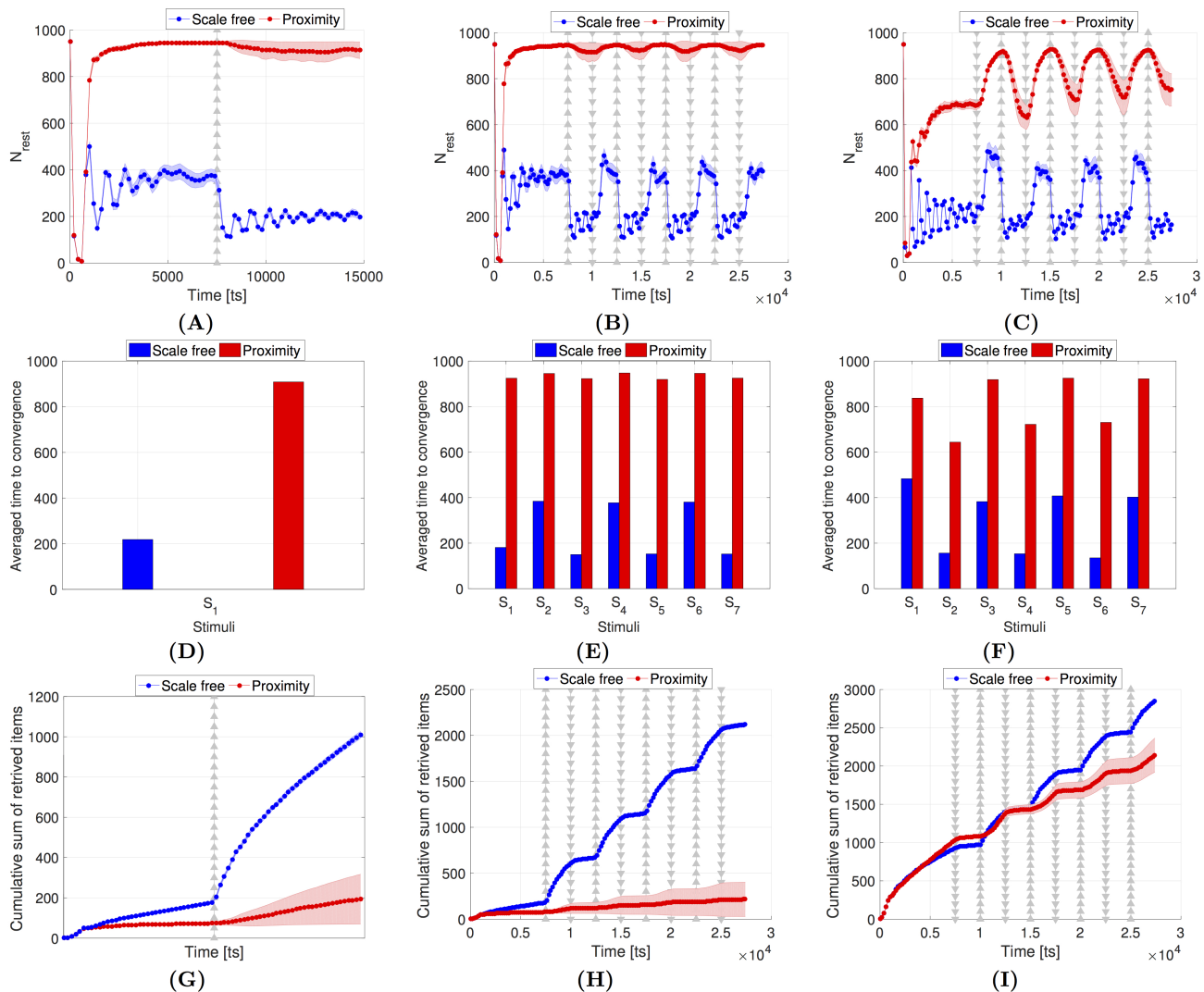


Figure 3. Swarm performance comparison between the scale-free networks (blue) and the proximity networks (red). **Top:** Swarm collective response in terms of N_{rest} . (A) single stimulus of item gain from $N_{items} = 30$ to $N_{items} = 300$ at $t_{crit} = 7500$ ts, and (B) multiple stimuli are executed in intervals of $\Delta t_{crit} = 2500$ ts. The items are repeatedly increased to $N_{items} = 300$ (indicated by Δ) or reduced to $N_{items} = 30$ (indicated by ∇). (C) Similar setting to (B), but starting from $N_{items} = 300$ and changing the items in an inverse order, as indicated by the Δ and ∇ markers. **Center:** Swarm convergence time. (D) Single stimulus of item gain, S_1 is the index for the stimulus applied at $t_{crit} = 7500$. (E) Multiple stimuli where items are repeatedly increased or reduced. $S_{1...7}$ correspond to the seven stimuli applied between $t_{crit} = 7500$ ts and $t = 25000$ ts in intervals of $\Delta t_{crit} = 2500$ ts, as in (B). (F) Similar to (E) but with an inverse order, as in (C). **Bottom:** Cumulative sum of the retrieved items. (G) Scenario with a single stimulus. (H) Scenario that starts with $N_{items} = 30$, as in (B). (I) Scenario that starts with $N_{items} = 300$, as in (C). In (A)-(C) and in (G)-(I), shaded areas indicate the confidence interval of 95%. All results were averaged over 30 runs.

308 proximity networks in Fig. 3B, this tendency towards the global resting state is due to the initial low density
 309 in food items (i.e. $N_{items} = 30$). Low N_{items} leads to a large number of failed attempts to find and retrieve
 310 them. Consequently, this increases $P_{f \rightarrow r}$ up to its maximum $P_{f \rightarrow r} = 1$, pushing the robots to keep resting.
 311 Thus, the subsequent increase in items to $N_{items} = 300$ is not sensed by the swarm. As an example, this
 312 behavior is evident at $t = 7500$ ts when N_{rest} did not decrease in response to the increasing N_{items} .

313 Therefore, it is important to consider the robustness of the swarm behavior to initial conditions, prior
314 to the external stimulus. To this end, we inverted the changes of N_{items} , starting with $N_{items} = 300$,
315 reducing it to $N_{items} = 30$ at $t = 7500$ ts, then increasing it back to $N_{items} = 300$, etc.. Under this specific
316 setting, foraging robots have a higher likelihood to find items than when the initial item density is as low
317 as $N_{items} = 30$. Consequently, the returning robots broadcast a larger number of “success” messages,
318 increasing the robots’ probability to switch to foraging ($P_{r \rightarrow f}$). Fig. 3C shows that this configuration of
319 the initial conditions led to an adaptive swarm behavior for the case of proximity networks. This adaptive
320 behavior comes with a reduced time to convergence (see Fig. 3F vs. Fig. 3E) and a significantly higher
321 number of retrieved items (see Fig. 3I vs. Fig. 3H). Nevertheless, with scale-free networks the collective
322 response not only remained more rapid but also appeared to be more robust to the initial conditions of the
323 system, as the trajectory of N_{rest} in Fig. 3C is qualitatively similar to Fig. 3B. Nevertheless, the scale-free
324 networks display higher fluctuations of N_{rest} compared to the relatively coherent decision achieved when
325 using proximity networks (Fig. 3A-C). This is due to the high impact that a single hub can have on a large
326 population of the swarm.

327 The key contribution of the network topology is reflected in the time the swarm requires to build up
328 its collective response. When using scale-free networks, hubs—i.e. robots with an exceptionally high
329 connectivity degree—help accelerate the information propagation in two manners: (i) due to their high
330 connectivity degree, their individual experience is shared with a large number of robots within one time step.
331 (ii) Their presence creates a shorter average path of the network compared to proximity networks, which
332 allows any two robots to exchange information over a smaller number of hops (i.e. within fewer time steps).
333 As mentioned above, we use the settling time defined in Eq. (4) to compute the swarm’s convergence time
334 after each stimuli—i.e. change in the items’ density. Fig. 3D shows the time it took the swarm to converge to
335 a steady number of resting/foraging robots after increasing the items at the foraging area from $N_{items} = 30$
336 to $N_{items} = 300$ at time step $\Delta t_{crit} = 7500$. Fig. 3E and F show the same measure for the repeated stimuli
337 of items increase and decrease, starting from $N_{items} = 30$ (Fig. 3E) and $N_{items} = 300$ (Fig. 3F). In all
338 three findings, Fig. 3D-F, we can notice the significantly shorter convergence time when robots in the nest
339 are communicating using the scale-free network in comparison to the proximity network. These results
340 suggest a higher level of swarm adaptivity to dynamic environments under scale-free communications.
341 Furthermore, as shown in Fig. 3G-I, using scale-free networks the cumulative sum of the retrieved items
342 is either considerably higher from the beginning or at the later stages of the experiment, compared to the
343 scenarios with proximity networks.

344 An important aspect to notice is the physical division between the site at which the information is to
345 harvest (i.e. the foraging environment), and the site at which the information is to exchange (i.e. the nest).
346 Usually, the communication speed is considerably higher than motion speed. However, specifically in the
347 foraging scenario, the communication speed is limited by the motion speed, since it is necessary for the
348 robot to travel across the foraging environment to reach the nest, where it can start communicating. One of
349 the clear consequences of this important remark is that even for the case of scale-free networks where the
350 collective response is accelerated, there is a considerably faster swarm reaction to an increase in the food
351 density compared to the reaction to a decrease (see the blue line in Fig. 3B). Before the increase of food
352 items, there were few foraging robots. Those robots consumed time to return to the nest, switch to resting,
353 inform their neighbors about their foraging experience, and, ultimately, convince more robots to leave the
354 nest in case of a successful foraging attempt. For scale-free networks this resulted in a rapid activation of
355 resting robots. Differently, collective reaction slowed down when the environmental change was a decrease
356 in food items. This behavior can be explained as follows: the large number of robots foraging while the
357 food density was high experienced the drop in the food density through their failed foraging attempts. Upon

358 returning to the nest, these robots led to considerably higher crowding at the nest entrance. This prolonged
359 the time that the robots needed to enter the nest and start communicating. Moreover, the higher N_{rest} the
360 higher the likelihood that there is one, giant, connected component inside the nest, spanning over a large
361 number of robots. If such a network is scale-free, the hubs have a high chance of influencing many robots
362 to switch to foraging. By contrast, a low N_{rest} often led to fragmented networks, reducing the influence of
363 hubs, lowering the number of switching robots and, thus, slowing down the collective response compared
364 to a high N_{rest} . Hence, the collective response time—even when using scale-free networks—is longer
365 when there are many robots foraging.

366 To obtain a closer look at the interaction network topology, we can analyze the degree distributions of
367 the resting robots interacting inside nest. We draw the degree distributions for different time steps that are
368 selected when the item density was both high (i.e. 300 items) and low (i.e. 30 items). As we can see in
369 Fig. 4A, scale-free networks strongly resemble a power-law distributed degree for all time steps at which
370 the networks are recorded. Similar consistent is the degree distribution of the proximity networks in Fig. 4B
371 for all tested time steps. However, the degree distribution here appears closer to a Gaussian distribution
372 which is more symmetrical around the mean than the scale-free network and has fewer outliers. To get
373 a clearer look at the outliers, in Fig. 4C-D, we show the communication degree using boxplots. For the
374 scale-free networks the density of outliers is notably large, the most extreme among those are the hubs
375 in the network. We can also notice a clear trend of a higher number of hubs when the number of resting
376 robots N_{rest} is higher due to low N_{items} . This density of outliers changes periodically between the external
377 stimuli S_i together with N_{rest} . In the case of proximity networks, the boxplots show a relatively low density
378 of outliers and negligible changes with S_i .

379 Additionally, it is worthwhile considering the effect of rewiring on the collective response. As elaborated
380 in Sec. 2.2, Alg. 1 is applied at every time step as the robots are in motion. However, because Alg. 1 has a
381 stochastic component, the resulting network at time step t is very likely to be different from $t - 1$. Such
382 dynamic rewiring increases the probability that two remote robots share a link. Consequently, a random
383 robot is more likely to obtain information from spatially uncorrelated sources, i.e. it obtains a sample that
384 is more representative of the swarm opinion. This resembles the common ‘random mixing’ paradigm often
385 found in swarm robotics, stating that an encounter probability between two robots is the same for any pair
386 of robots. Thus, the adaptive behavior that follows from using Alg. 1 could be largely attributed to this
387 rewiring-induced opinion mixing.

388 To examine whether this may indeed be the case, we ran simulations with a modified version of Alg. 1
389 where we replaced the preferential attachment component $d_s / \sum_i d_i$ by a real number $\rho \in \{0.01, 0.1\}$. Note
390 that while this modification aims at altering the network topology, the resulting alternative networks are
391 still regenerated at each time step, similar to scale-free networks, i.e. the notion of rewiring is preserved.
392 The results are shown in Fig. 5. The similarity to the scale-free networks scenario is particularly striking for
393 $\rho = 0.01$. When N_{rest} is low, it becomes difficult to separate a scale-free network (where the degrees are
394 power law distributed) from a small-world network (where the degree distribution is much less skewed, i.e.
395 more symmetric around the mean value). Therefore, for low N_{rest} the impact of the preferential attachment
396 component in Alg. 1 can be well approximated by a constant such as $\rho = 0.01$. More importantly, it shows
397 that the strong effect that dynamic rewiring has on swarm adaptivity and collective response.

398 A feature that frequently occurs in realistic communication is the packet loss. It occurs when a robot fails
399 to receive a message broadcast by a neighbor, due to radio-frequency interference or due to overflow of
400 a robot’s receiver queue. We implemented packet loss events by allowing the robots to ignore incoming
401 messages with probability p_{pl} . Fig. 6 shows the results for the proximity and scale-free networks with

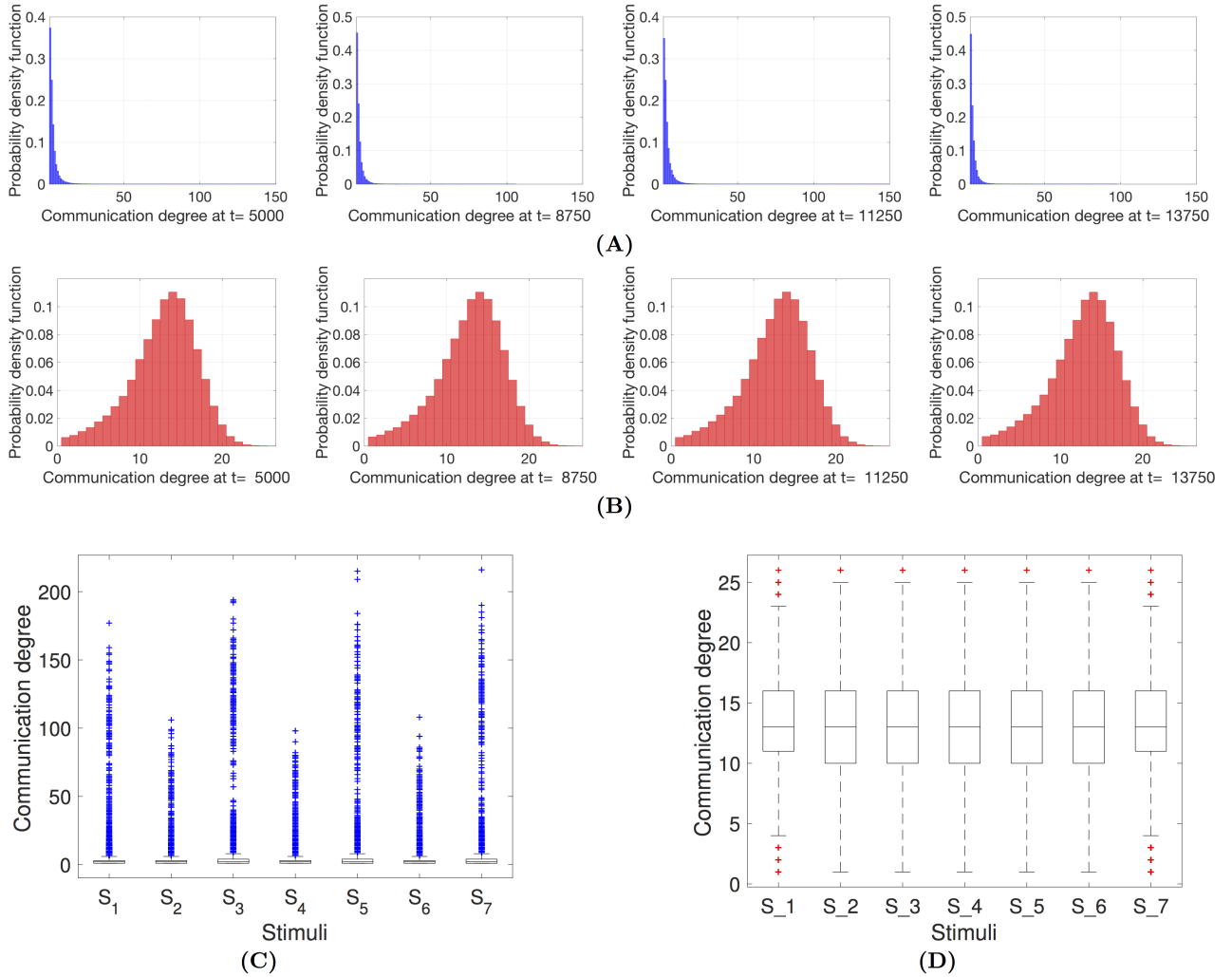


Figure 4. Degree distributions of the networks within the nest at different time instances. (A) Scale-free networks; (B) Proximity networks. At $t = 5000$ ts and $t = 11250$ ts there are $N_{items} = 30$ to retrieve, while at $t = 8750$ ts and $t = 13750$ ts the item count is $N_{items} = 300$. Additionally, box plots for the (C) scale-free and (D) proximity networks illustrate the presence of outliers for the different onsets of stimuli $S_{1...7}$ (starting at $t_{crit} = 7500$ ts and occurring in intervals of $\Delta t_{crit} = 2500$ ts). As expected, in contrast to the proximity networks, in case of scale-free networks, the outliers (indicated by the + markers) are so extreme that the boxes containing the mean values are barely recognizable at the bottom of plot (C).

402 $p_{pl} \in \{0.1, 0.5\}$. Surprisingly, the swarm adaptivity considerably improves in case of proximity networks,
 403 while with scale-free networks the swarm remains more robust to the influence of the packet loss. Higher
 404 probabilities of packet loss appears to shorten the time to convergence and slightly increase the number
 405 of collected items. One possible explanation for this behavior could be that by probabilistically ignoring
 406 incoming messages the robots become to some extent able to reduce the correlation between their behavior
 407 and that of their spatial neighbors. Synthetically generated networks, such as the scale-free networks
 408 considered in this study, represent an extreme case of such spatial decorrelation. In contrast, in proximity
 409 networks and absence of packet loss, spatial correlations are very high, leading to feedback mechanisms
 410 that reduce sensitivity to new information. The presence of packet loss appears to create a middle ground
 411 that bolsters the adaptive behavior at the swarm level. However, we only tested two values of p_{pl} and it is
 412 possible that for $p_{pl} > 0.5$ inverse effects could be observed. Finally, when resting state can be associated

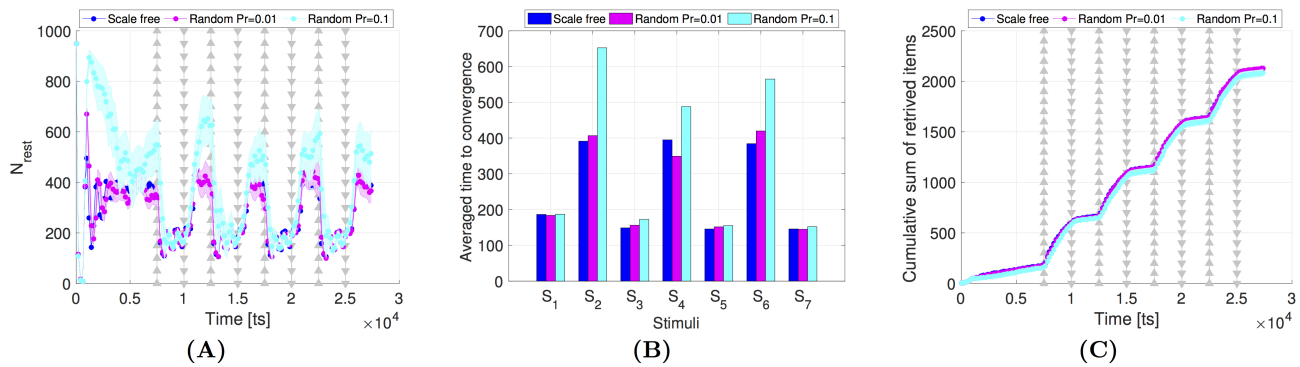


Figure 5. Comparison of the (A) swarm collective response, (B) time to convergence and (C) swarm performance, between scale-free networks and random networks created with $\rho = 0.01$ and $\rho = 0.1$.

413 with low energy consumption, the behavior of the system in the presence of here considered p_{pl} may
 414 demonstrate a high level of efficiency, in terms of increasing N_{rest} while preserving the high number of
 415 retrieved items. Nevertheless, as mentioned above, the detailed investigation of the influence of packet
 416 loss is beyond the scope of the current study and future research is needed to confirm the generality of
 417 our findings⁵. Moreover, here we consider constant values of p_{pl} that are the same for every robot in the
 418 swarm and that do not change based on the location of the robot or the number of communication links. In
 419 contrast, in more realistic settings not only the packet loss but also p_{pl} itself may have fluctuating values
 420 depending on the situation and both could be profoundly difficult to control.

421 Finally, we compare the intensity of the collective response resulting from different social cues. As
 422 mentioned above, social cues are the main driver of the dynamics to build up a faster response over the
 423 interaction network. Our results show that higher social cues lead to a higher activation of the resting
 424 robots, see Fig. 7 that shows the activation of the resting robots when setting $s_f = 0.99$, $s_r = 0.99$ in
 425 comparison to the setting $s_f = 0.01$, $s_r = 0.01$ (results are averaged over 30 runs). High social cues
 426 activate considerably more resting robots (i.e. reduces number of resting robots) than low cue values
 427 (Fig. 7A). However, the convergence time with high cue values is comparable to the previously considered
 428 default case of $s_f = s_r = 0.25$ (see Fig. 7B). The number of collected items overlaps for all three cue
 429 values (see Fig. 7C).

4 CONCLUSION

430 The goal of this study is to investigate the role of network topology in influencing the propagation of
 431 information in a foraging scenario with changing the availability of food items. Therefore, we have
 432 addressed scenarios with dynamic environments, a realistic aspect of most real-world applications. We
 433 considered two types of changes: a single abrupt change (referred to a single stimulus) and periodic
 434 changes (multiple stimuli). We aimed to examine how scale-free networks, in particular, may accelerate the
 435 spreading of information and hence enable a quicker collective response than proximity networks to the
 436 global changes.

437 We have implemented scale-free networks across the robots resting in the nest, as the nest is usually
 438 the part of the environment in which communication takes place. We applied the well-known preferential

⁵ To this end, the interested reader is encouraged to use our publicly available resources provided on <https://osf.io/48b9h/>.

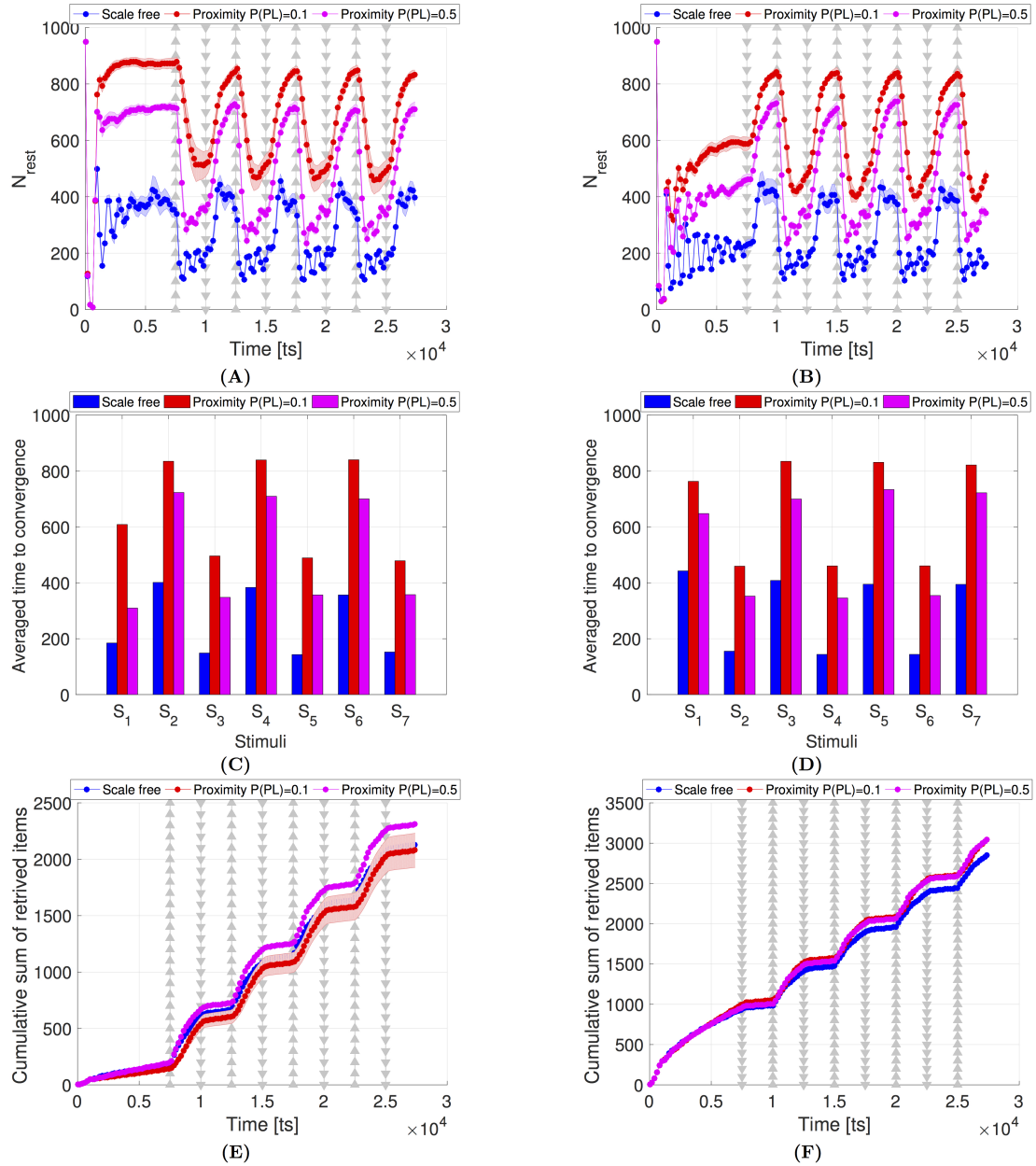


Figure 6. Swarm performance comparison between the scale-free networks (blue) and the proximity networks in presence of packet loss, with packet loss probability $p_{pl} = 0.1$ (red) and $p_{pl} = 0.5$ (magenta). The number of items is repeatedly increased to $N_{items} = 300$ (indicated by \triangle) or reduced to $N_{items} = 30$ (indicated by ∇). These repeating changes occur in intervals of $\Delta t_{crit} = 2500$ ts, starting at $t_{crit} = 7500$ ts. **Left column:** Scenario with initially $N_{items} = 30$. **Right column:** Scenario with initially $N_{items} = 300$; (A)-(B) Swarm collective response in terms of N_{rest} . (C)-(D) Swarm convergence time. $S_{1...7}$ correspond to the seven stimuli between $t_{crit} = 7500$ ts and $t = 25000$ ts. (E)-(F) Cumulative sum of the retrieved items. In (A),(B),(E) and (F), the shaded areas indicate the confidence interval of 95%. All results represent averages over 30 runs.

439 attachment technique to construct the scale-free topology. Following preferential attachment, the probability
 440 of connecting to a robot is proportional to its current connectivity degree. Therefore, a number of robots
 441 emerge to have a relatively high degree of connectivity, those are referred to as the hub robots. When
 442 the density of food items changes at the foraging environment, and this change is reflected in the robots'

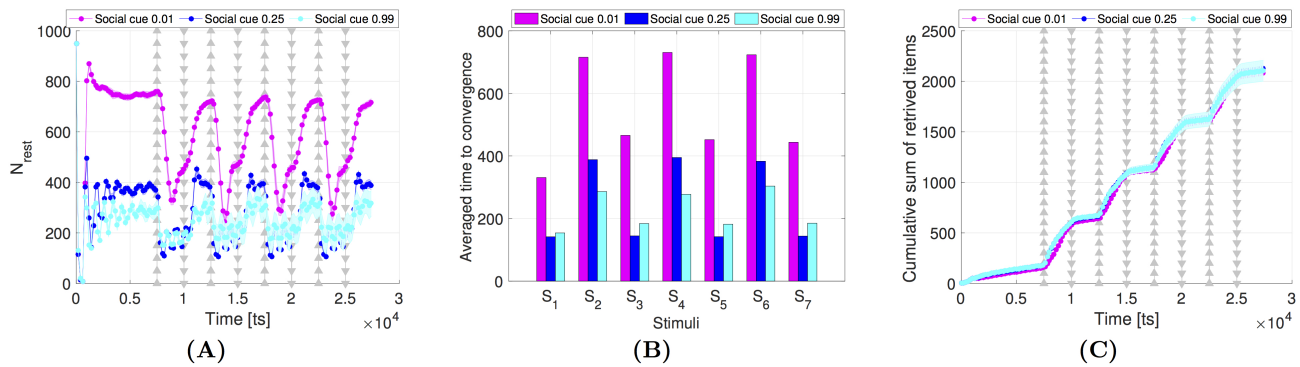


Figure 7. Comparison of the (A) swarm collective response, (B) time to convergence and (C) swarm performance, between different values of social cues for swarms communicating through scale-free networks. Apart from $s_f = s_r = 0.25$ we consider two extreme cases: low values ($s_f = s_r = 0.01$) and high values of social cues ($s_f = s_r = 0.99$). All results were averaged over 30 runs.

443 experience, scale-free networks enable a faster spreading of this information in the nest. This led to a
 444 faster collective response compared to the scenarios in which interactions between the resting robots were
 445 implemented using proximity networks.

446 Our results suggest that the use of scale-free networks can improve the collective response of the swarm
 447 to changes in their dynamic environment, by improving the spread of shared information and reducing the
 448 spatial correlation in the robots' decisions. These two desired features in collective systems are achieved
 449 due to the introduced possibility to communicate over long distances, as well as due to the dynamic
 450 rewiring of the interaction network at every time step as a consequence of robot motion. These insights
 451 were obtained by comparing the swarm behavior in scenarios with and without systematic packet loss,
 452 in addition to comparing the swarm performance between scenarios with scale-free networks and with
 453 alternative random networks. Furthermore, our findings showcase the effect of social cues on the intensity
 454 of the collective response in presence of scale-free networks. Our results show that higher social cues lead
 455 to a higher activation of the resting robots, due to the increased influence of their neighbors' experience.

456 Although scale-free networks have shown to equip the swarm with a quicker reaction to changes in
 457 dynamic environments—studied for the collective foraging task—this came at the cost of the coherence of
 458 the collective response. Scale-free topologies led to more fluctuations of the swarm decision (whether to
 459 rest or to forage). These fluctuations can be explained in terms of the high influence of particular individuals
 460 (i.e. the hubs) on the opinions of a large population of the resting robots. Two particularly promising
 461 research directions for future work include the design of self-organized algorithms to implement scale-free
 462 topologies in robots swarms. Additionally, the design of efficient individual decision mechanisms that
 463 helps the collective response to demonstrate a higher stability. Finally, generalizing this study to other
 464 collective tasks such as site selection, flocking, and others may also lead to new interesting insights.

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CONFLICT OF INTEREST STATEMENT

550 The authors declare that the research was conducted in the absence of any commercial or financial
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552 interests.

AUTHOR CONTRIBUTIONS

553 All authors contributed conception and design of the study; PS provided funding and administered
554 the project; YK and PS supervised the study; IR implemented the simulation setup, performed the
555 simulations and the formal data analysis; YK wrote the first draft of the manuscript; YK and IR continuously
556 discussed and elaborated on the design parameters and obtained results, which led in some cases to further
557 implementations and analysis. YK and IR wrote most sections of the manuscript and analyzed the
558 experimental data. IR and YK critically reviewed and edited the manuscript. All authors approved the
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DATA AVAILABILITY STATEMENT

560 The original contributions presented in the study are publicly available. This data can be found here:
561 <https://osf.io/48b9h/>.